

AUC 2022 workshop Membrane Proteins

Sedimentation velocity for membrane proteins

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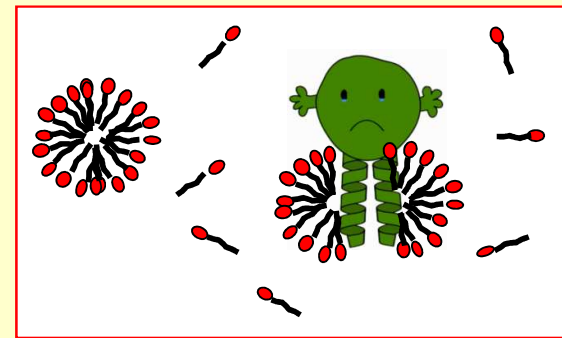
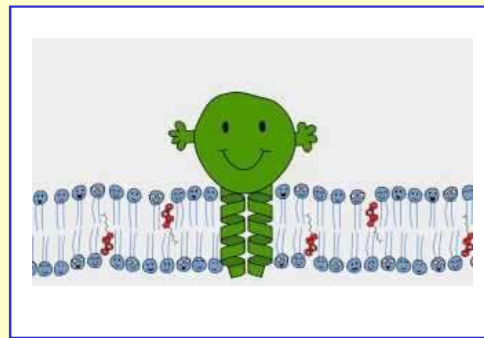
Membrane Proteins

- One third of the expressed proteins
- Essential for the life of the cell
- Target of more than 50% of the drugs.
- Still difficult to obtain high resolution structures

Solubilisation & purification of membrane proteins require detergent

- Associated inactivation & Instability

=> New surfactants / detergents

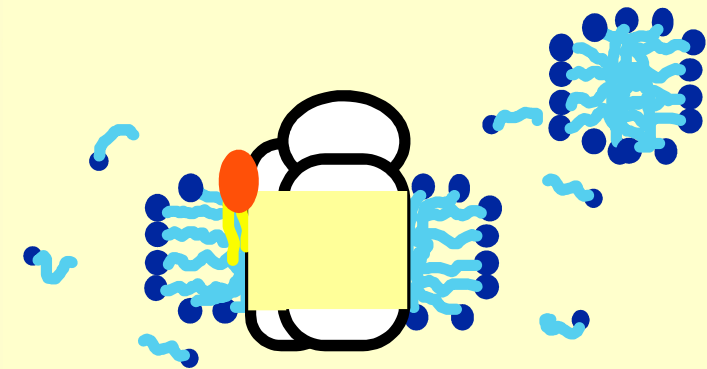


Cartoon adapted from <http://sbcb.bioch.ox.ac.uk/memprotmd/beta/>

- Heterogeneous and multicomponent systems

=> Specific methods for studying composition, interactions

	Separation	# signals	# contrasts	Mass Compo	Shape	Structure
SEC-MALS	Y	Y		Y	Y	
AUC		Y	Y	Y	Y	Y
SANS		Y	Y	Y	Y	Y



Membrane proteins

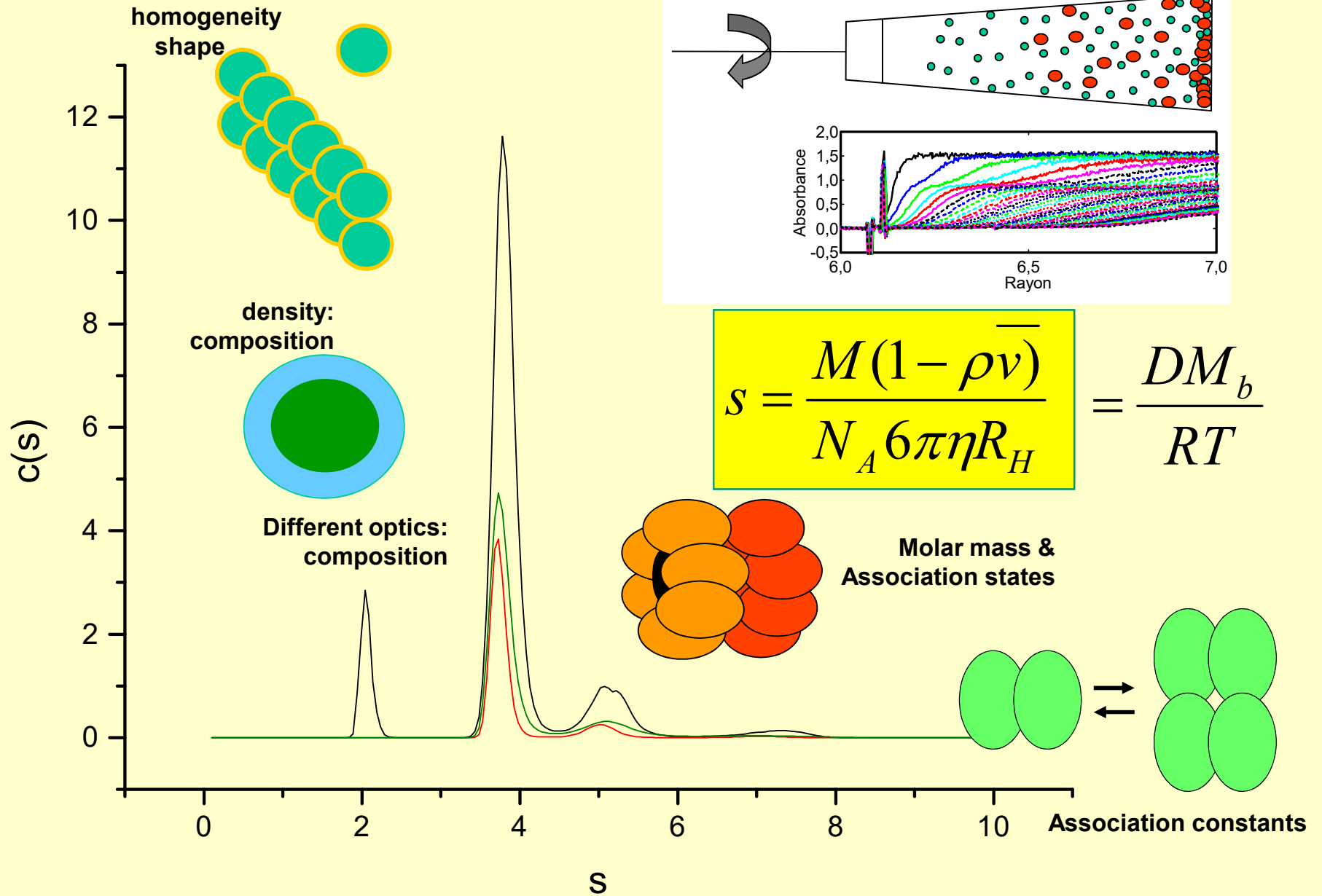
1) AUC, Summary

2) The specificity of membrane proteins

3) Strategy & protocols

4) Examples

Analytical Ultracentrifugation Sedimentation Velocity



SV: velocity of the particles

SE
particle distribution at equilibrium

buoyant mass = mass + relative density

$$M_b = M(1 - \rho \bar{v})$$
$$= \sum M_i (1 - \rho \bar{v}_i)$$

$$s = \frac{M_b}{N_A 6\pi\eta R_H}$$

shape

R_H , or D , or f , or f/f_{\min}



- $c(s)$ analysis $\Rightarrow s$. Then, if R_H is known $\Rightarrow M_b$
- Non interacting species analysis: $\Rightarrow s$ and $R_H = M_b$
- Sedimentation equilibrium analysis $\Rightarrow M_b$

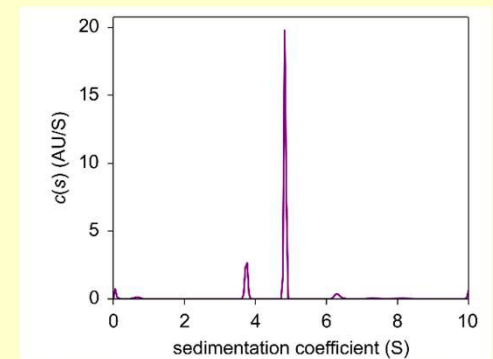
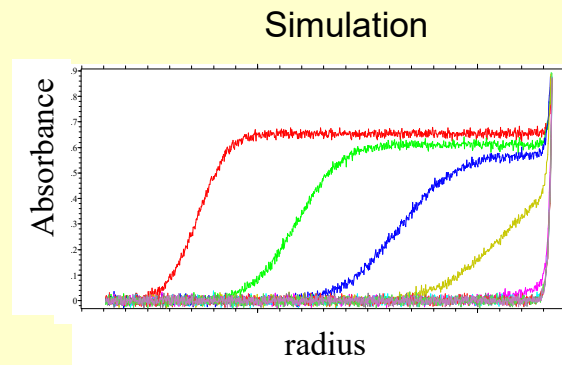
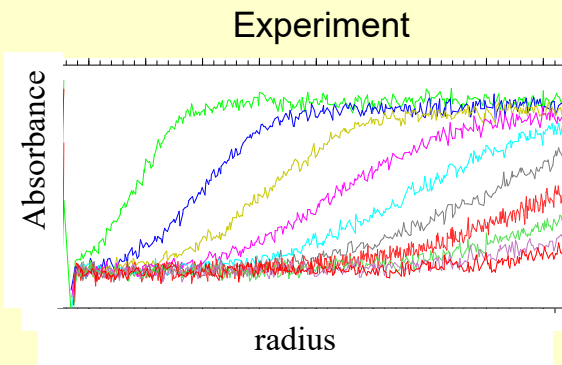
Then,
information
on composition
is required for
 $M_b \Rightarrow M_{\text{prot}}$

Principle of sedimentation velocity data analysis

Lamm equation, for each type of particles

$$\left(\frac{\partial c}{\partial t}\right) = - \frac{1}{r} \frac{\partial}{\partial r} \left[r(c s \omega^2 r - D \frac{\partial c}{\partial r}) \right]$$

- Data analysis are based on numerical solutions of the transport equation. i.e. simulations
- They compare simulated profiles (with given s - and D - values) to experimental ones.



- In the $c(s)$ analysis, we consider a distribution of particles, for which a plausible relationship between s and D is established (input : v , f/f_{\min} , ρ and η): only concentrations and noises are determined.
 - high resolution distribution of sedimentation coefficients, s .
- In the non-interacting species analysis, s , D , concentrations and noises are adjusted.
 - s and D (thus R_H), thus s and M_b



Interacting system: several or one boundaries

- **In a slow equilibrium** the different species sediment as non-interacting species in proportion related to the dissociation constant for the loading concentration.
- **In a fast or intermediate equilibrium** between different species, the slow boundary reflects the sedimentation of one of the species. The fast boundary is a “reaction boundary” and its value does not reflect the sedimentation of the complex.

s_{mean} can be used for the calculation of the K_D

$$s_{\text{mean}} = \frac{\sum c_i s_i}{\sum c_i}$$

c_i : concentration of component i in g/l,
 s_i the corresponding sedimentation coefficient.

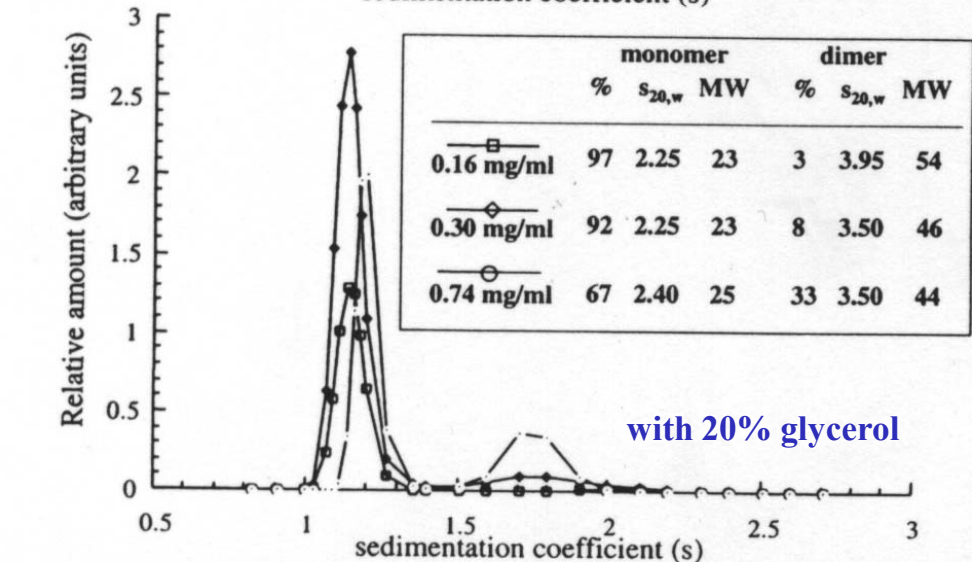
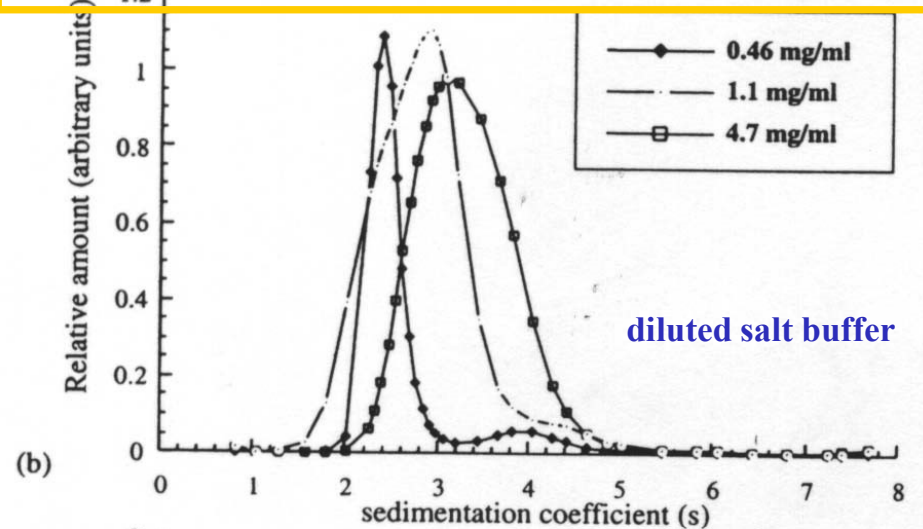
The regime depends on k_{off} = off-rate constant (s^{-1})

$\log_{10}(k_{\text{off}}) =$

- -1 : can be considered infinitely fast in the context of SV.
- -3 : still fast, but on the limit where kinetics should significantly influence the boundary pattern.
- -3.4 : intermediate.
- -4 : in the slow regime, but still influenced by kinetics.
- -6 : essentially infinitely slow on the SV time-scale.

Zhao et al Methods 54, 16-30 2011

Epstein Virus Protease Monomer- dimer equilibrium *Buisson 2001*

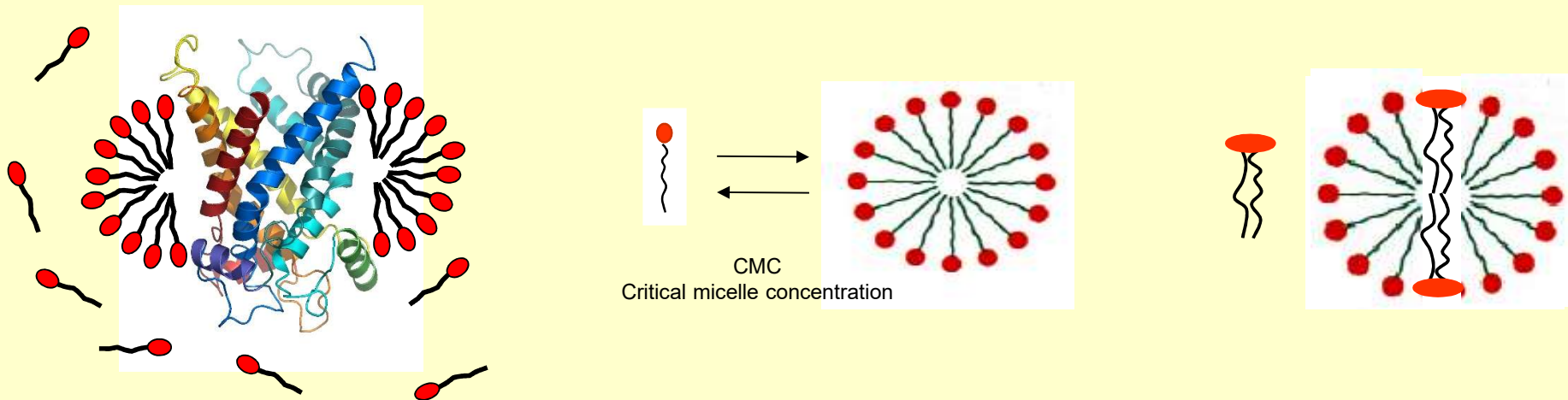


1) AUC, Summary

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- 1: Complex = protein-detergent-lipid.: composition generally unknown
- 2: Detergent-lipid micelles: concentration often unknown; often they do not absorb at 280nm; lipids content unknown.

Detergent	Bacteriorhodopsin		Ca ²⁺ -ATPase	
	Gram/g	Mol/mol	Gram/g	Mol/mol
Triton X-100	2.9	124	0.44	77
C ₁₂ E ₈	2.4	119	0.50	103
DM	4.1	207	0.73	152
DDAO			0.5	240

Møller, J. V. & le Maire, M. (1993)

Integration of the $c(s) \Rightarrow$ Signals : A_{280} and ΔJ for each species

$$\Delta J = \left(\frac{\partial n}{\partial c} \right) / \lambda \cdot l \cdot c$$

ΔJ : fringe shift, λ : laser wavelength
 l : pathlength ; c : concentration (weigh unit)

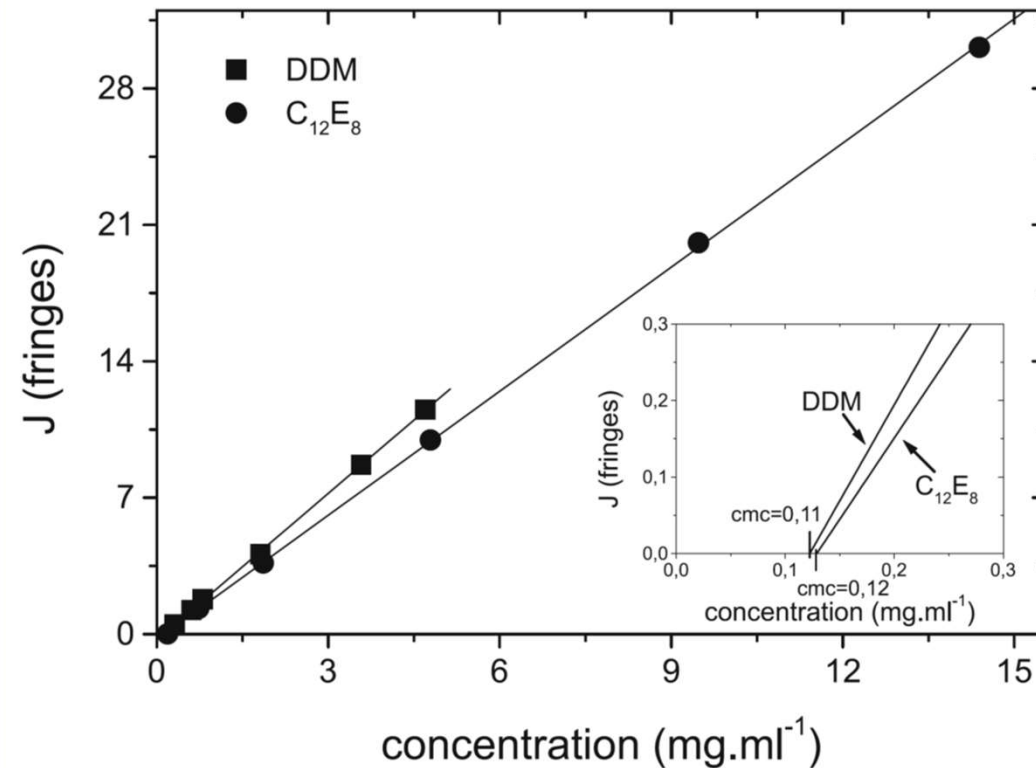
$$A_{280} = \varepsilon_{280} \cdot l \cdot c$$

A_{280} : Absorbance, ε_{280} : extinction coefficient at 280 nm

Membrane proteins bound (det.+ lip.) : $\delta_{DL} = (\delta_D + \delta_L)$

	$\frac{\partial n}{\partial c}$ mL g ⁻¹	reference	ε_{280} cm ⁻¹ mg ⁻¹ mL
Membrane protein	0.187	Hayashi 1989	typically 1
C12E8	0.134		≈ 0
C12E8	0.121	Salvay 2006	≈ 0
DDM	0.143		≈ 0
DDM	0.133	Strop 2005	≈ 0
FOS14	0.133		≈ 0
LDAO	0.148		≈ 0
Triton X100	0.154	Csu'cs 1998	2.31
Lipid	0.083		≈ 0
DMPG	0.127	Karin 1997	≈ 0
F6-MonoGlu	0.068	Breyton 2009	≈ 0

Detergent $(\frac{\partial n}{\partial c})$ and CMC



Salvay 2006

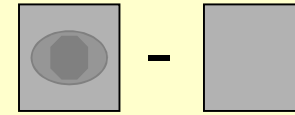


ε_{280} very often ill-defined
 for membrane proteins
 \Rightarrow Erroneous δ_{DL} from A_{280} and ΔJ

Buoyant properties of the detergent

Partial specific
volume \bar{v}^*
(ml.g⁻¹)

Buoyant factor
($1 - \rho^{\sigma} \bar{v}$)
in water



Protein

0.74

0.26

SDS

0.86

0.13

DDM

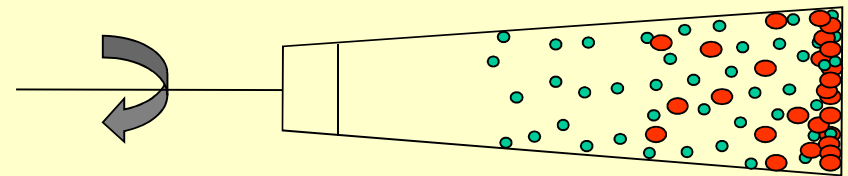
0.83

0.17

F6-Monoglu*

0.57

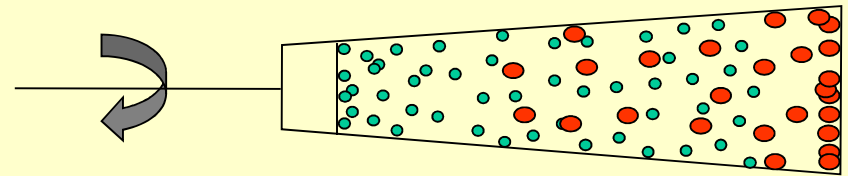
0.43



DDAO

1.13

-0.13



LAPAO*

1.002

0

C₈E₅:

0.997

0.003

Octyl POE:

0.99

0.01

C₁₂E₈:

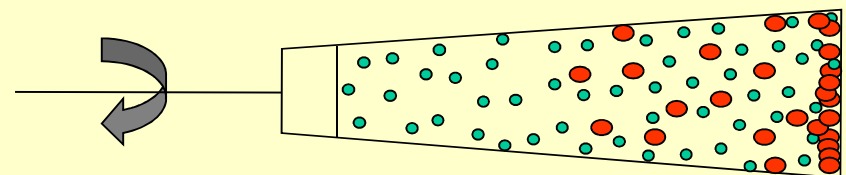
0.97

0.03

Lipid

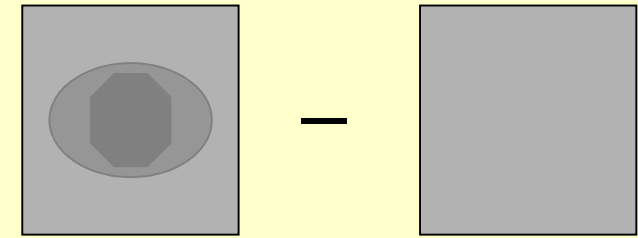
≈ 1; 0.981*

≈ 0 as a mean ; 0.02*



*Ie Maire et al.(2000), except F6-Monoglu: Breyton 2006; LAPAO: Nury 2008; lipid: Huan 1971.

$$M_b = M_{PD} \cdot (1 - \bar{v}_{PD} \rho^\circ)$$



==> compare with calculated M_{PD}, \bar{v}_{PD}
 ==> measurement at two solvent densities => M_{PD}, \bar{v}_{PD}

$$M_b = M_P \cdot (1 - \rho^\circ \bar{v}_P) + \delta_D M_P \cdot (1 - \rho^\circ \bar{v}_D) + \delta_L M_P \cdot (1 - \rho^\circ \bar{v}_L)$$

Protein

Detergent

Lipid

Can be masked if $(1 - \rho^\circ \bar{v}_D) = 0$

Negligible in water

==>> Compare with calculated M_b for the components
 ==>> Contrast density variation in H_2O/D_2O
 ==>> Estimates of δ_D from SV or other techniques (SEC with radiolabelled detergents...)

$$M_b = M_p \cdot \left(\frac{\partial \rho}{\partial C_P} \right)_\mu$$

Can be measured by precise density
 (After chromatography / dialysis)

1) AUC, Summary

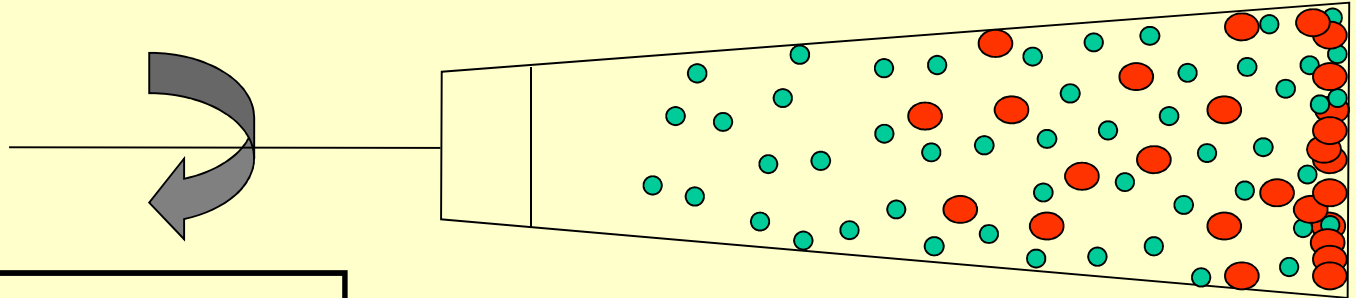
2) The specificity of membrane proteins

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STRATEGY

First, always: Sedimentation velocity: $c(s)$



From sedimentation velocity experiments at 3 concentrations

Distribution of sedimentation coefficients

$c(s)$

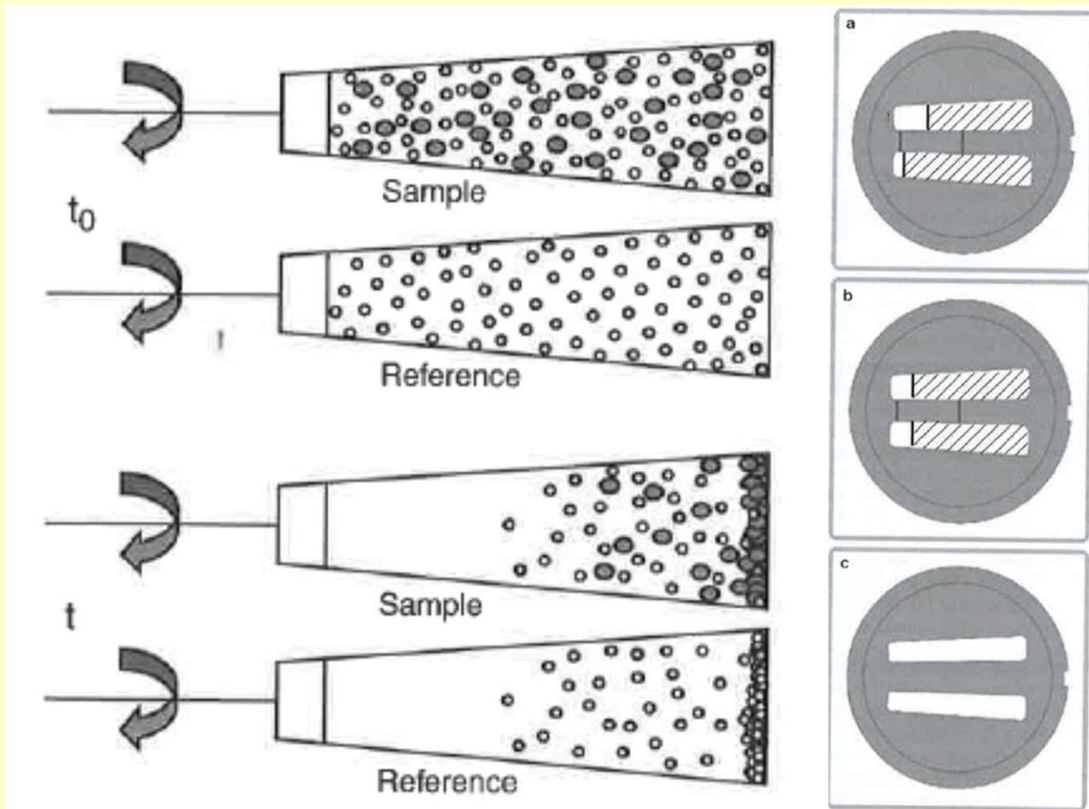
- homogeneity?
- interactions?
- possibility of SE experiments?
 - bound (detergent+ lipid)
 - free detergent concentration
 - association state from $s + R_H$ or/and from $s + f/f_{\min} = 1.25$
- Experiments in $H_2O + D_2O \Rightarrow \bar{v}_{PD}$

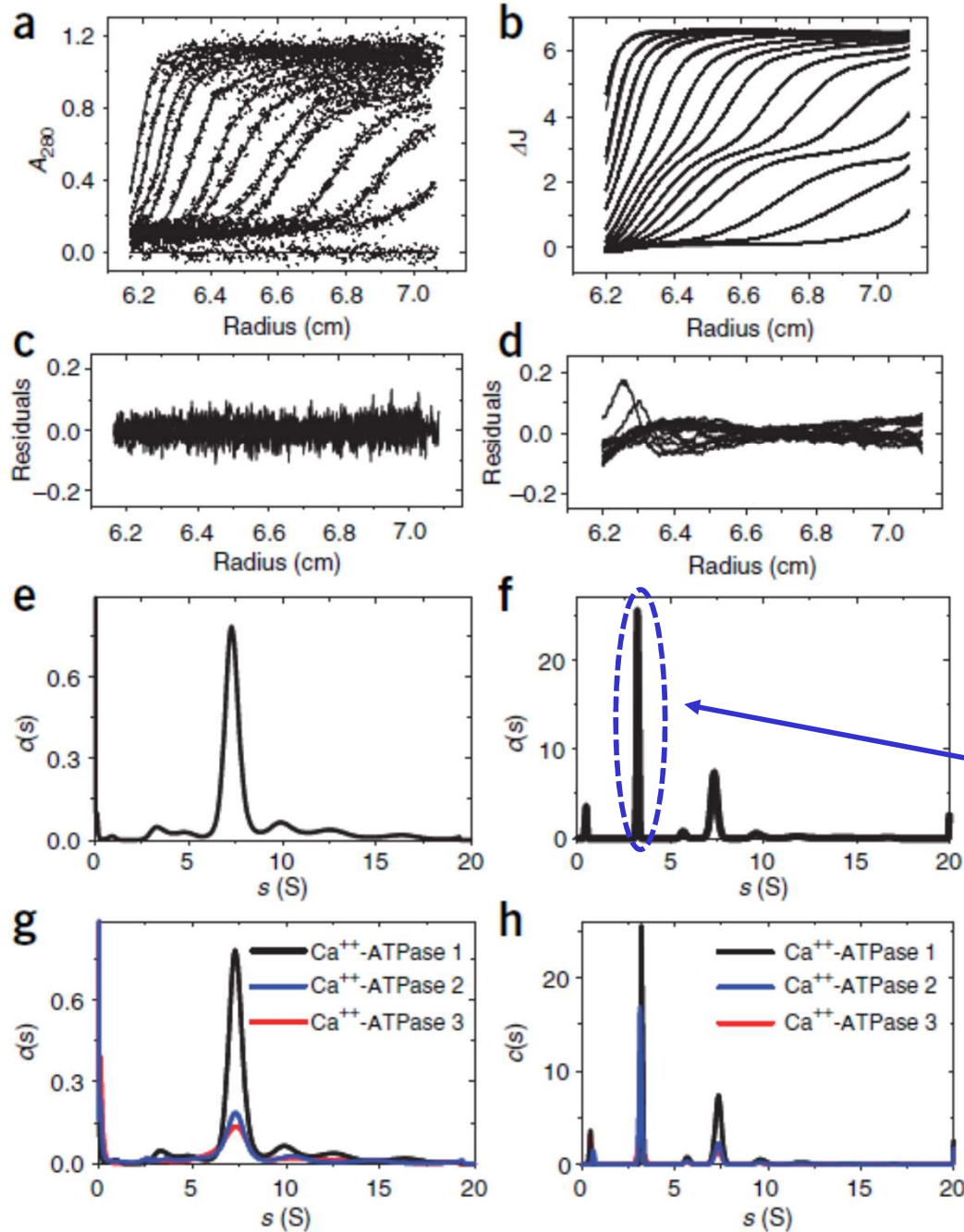
Proposed experimental protocol

- SV at different concentrations: dilution in solvent with and without detergent.
- measurement absorbance + interference.
- Recommended : **NO detergent** in the reference compartment:
detergent micelles sediment as particles
- If required (if e.g. glycerol...): exp after dialysis or solvent exchange columns and using double sector capillary type centerpieces to fix the same free detergent concentration in the two channels

For the analysis

Use all knowledge
(bound detergents, lipids, R_H)





Having no detergent in the reference channel allows to measure the free detergent concentration

1) AUC, Summary

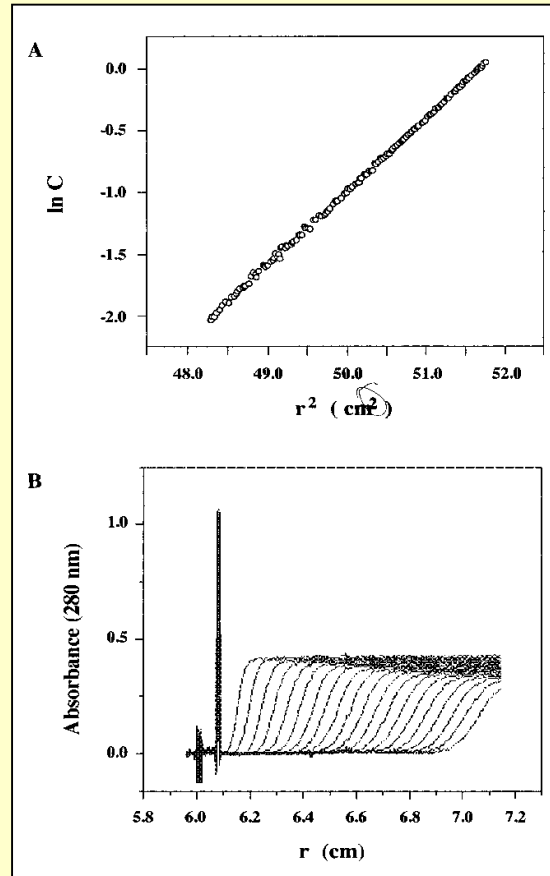
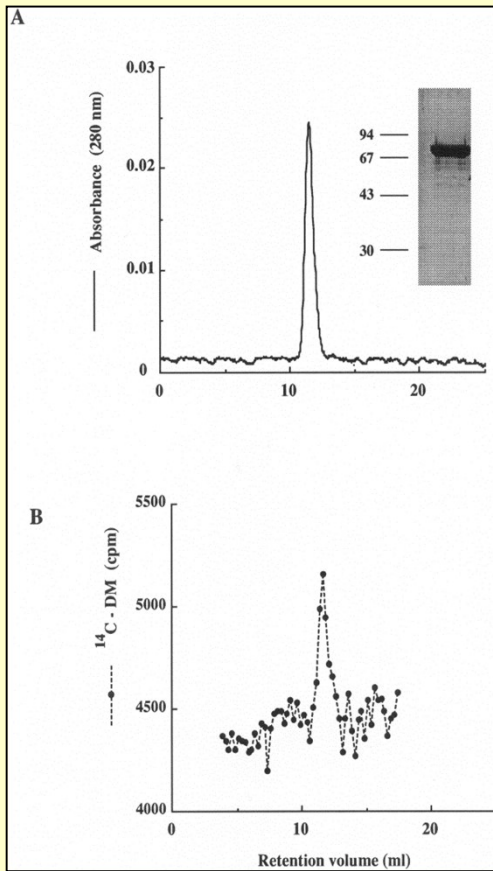
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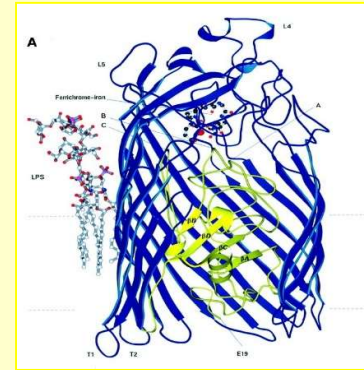
4) Examples

- FhuA : SV at 280nm + SEC with radiolabeled DDM
- Change of $c(s)$ with protein & detergent concentration
- Using different optics
- SV in H₂O and D₂O

FhuA / DDM



Boulanger et al. (1996)
Biochemistry 35, 14216-14224



Ferguson et al.,
Science, 1998, 282, 2215

Size exclusion chromatography + ^{14}C labelled detergent
 AUC SE and SV at 280nm

- $\delta_D = 1.2$ g/g
- $R_H = 4.2$ nm
- $M_b = 185$ kDa
- $s_{20,w} = 7.8$ S

$$M_b; \delta_D \Rightarrow \begin{matrix} M_{PD} = 185 \text{ kDa} \\ M_P = 84 \text{ kDa} \end{matrix}$$

$$s_{20,w}; \delta_D; R_H \Rightarrow \begin{matrix} M_{PD} = 172 \text{ kDa} \\ M_P = 78 \text{ kDa} \end{matrix}$$

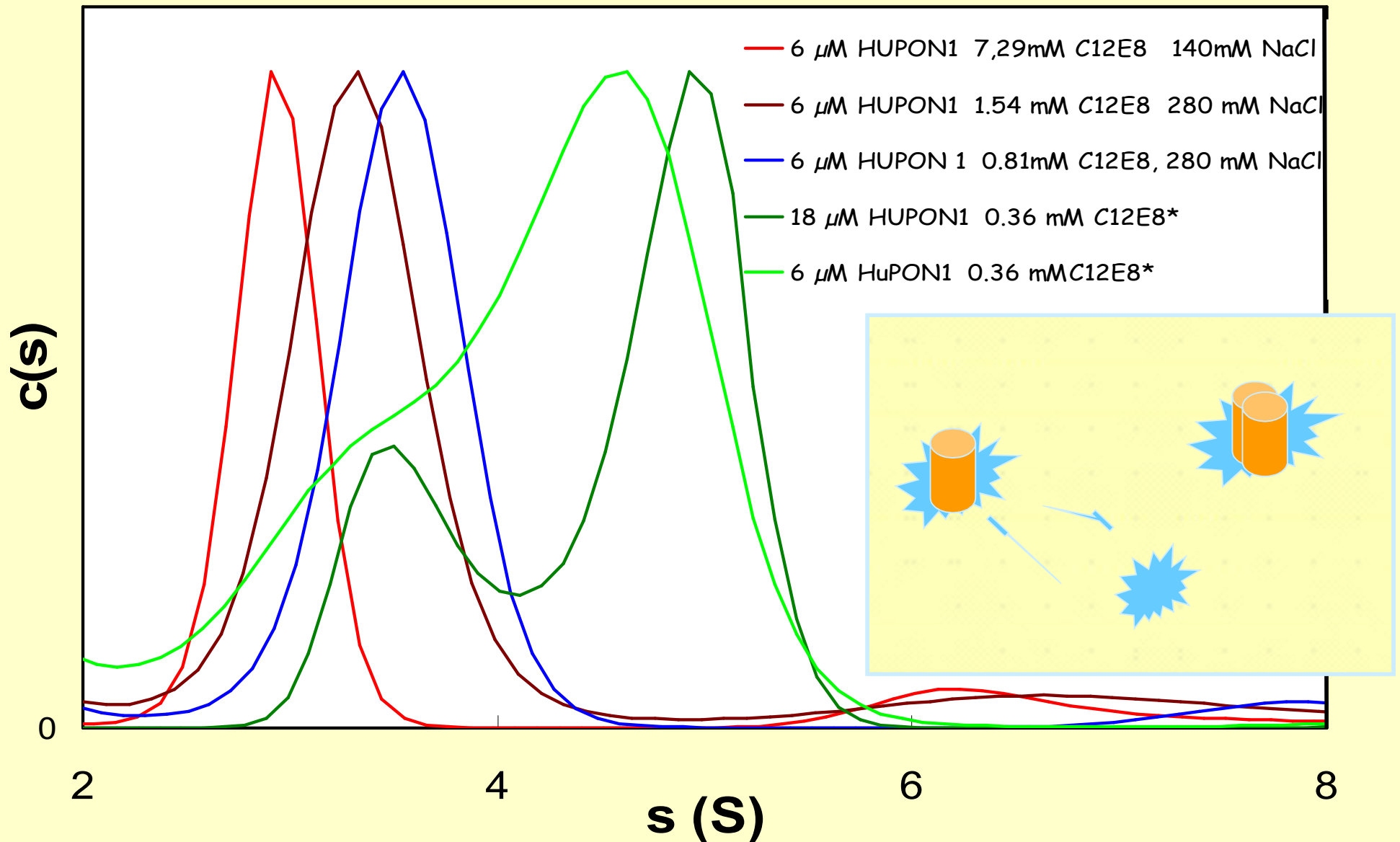
$$s_{20,w}; M_b \Rightarrow R_H = 4.5 \text{ nm}$$

$$R_S; \text{compo.} \Rightarrow f/f_{\min} = 1.18$$

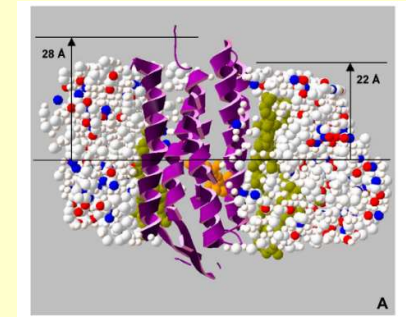
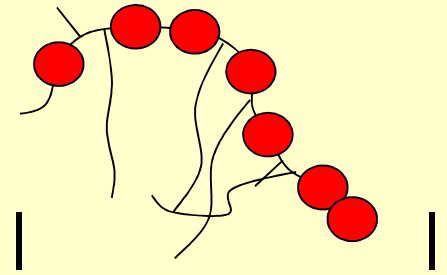
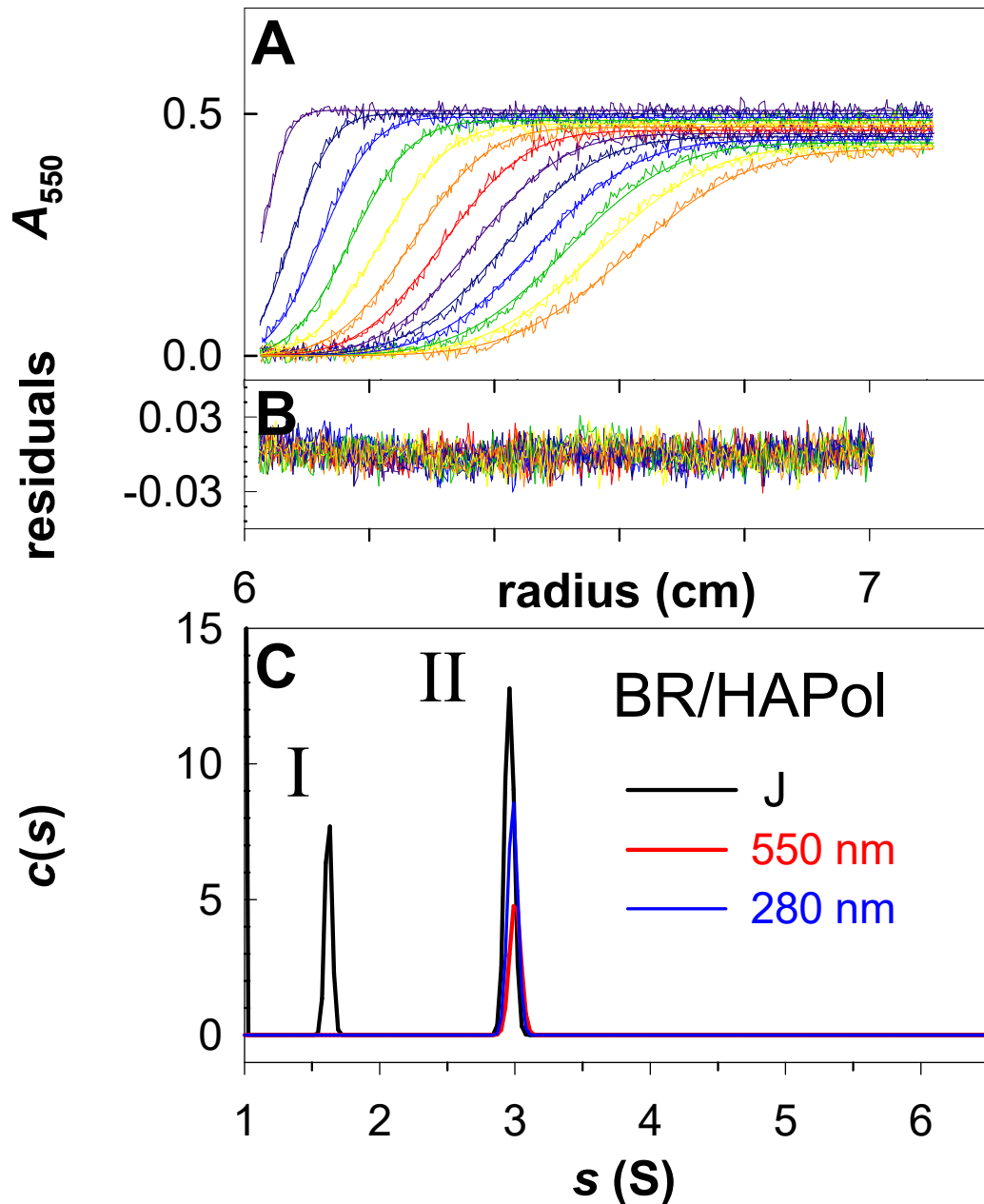
$$M_{\text{seq}} = 79 \text{ kDa}$$

SV AUC Hupon in $C_{12}E_8$

HuPON 1 auto-association is modulated by detergent



Using different optics for characterizing Apol/BR complexes

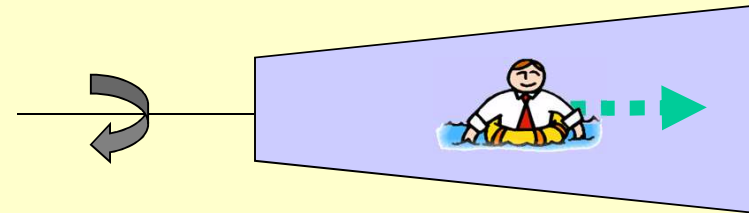


Free APol/BR:
- 0.4 g/g from J

BR Complexes:
- homogeneous or close to homogeneity.
- Native BR from A_{280}/A_{555}
- (APol+lipid)/BR ~ 2.2 g/g from J/A_{280}
- Bound lipids 0.4 g/g from lipid analysis

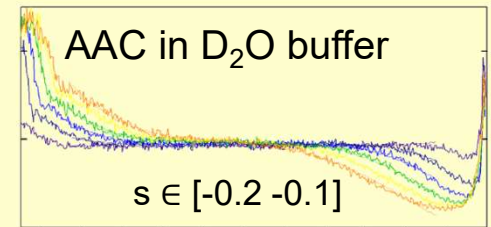
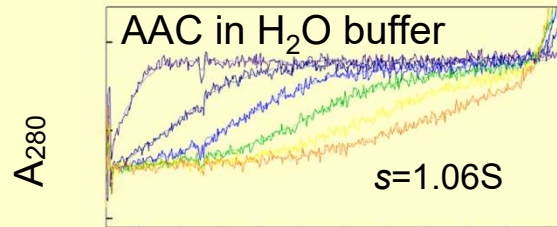
TOOL: integrating the $c(s)$ from A_{280} and J for determining the bound surfactant + lipid amount now available in Gussi Brautigam et al., 2015

SV in H₂O and D₂O solvents



Hypothesis: same shape; same composition

- M changes to M_D (exchangeable H)
- \bar{v} is defined for hydrogenated material
- R_s does not change
- solvent density and viscosity change



$$s_H = M_p \left[(1 - \rho_H \bar{v}_p) + \delta_d (1 - \rho_H \bar{v}_d) \right] / N_A 6 \pi \eta_H R_s;$$

$$s_D = M_p \left[\left((M_D/M)_p - \rho_D \bar{v}_p \right) + \delta_d \left((M_D/M)_d - \rho_D \bar{v}_d \right) \right] / N_A 6 \pi \eta_D R_s.$$

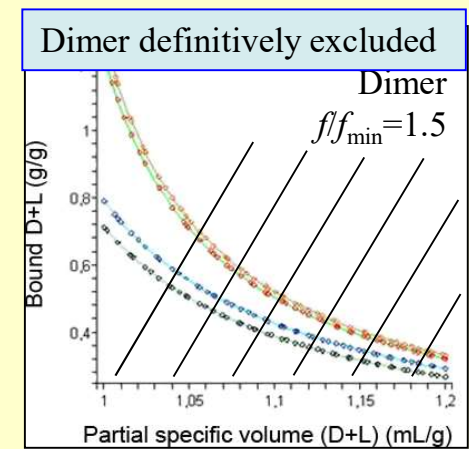
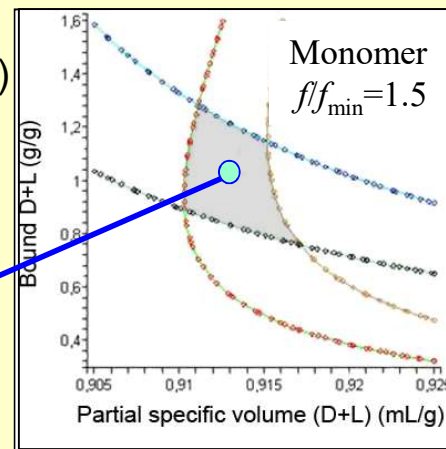
The s_H/s_D method

A graphical representation to investigate:
Is a given association state of the protein (monomer, dimer) compatible with the sedimentation coefficients measured in H₂O and D₂O buffer?
Useful when lipid is bound in ill-defined amount

$\bar{v}_{d+l} : 0.92 \text{ ml/g}$
 $\delta_{d+l} : 1.1 \text{ g/g}$

$ff_{\min} : \text{realistic}$

$\bar{v}_{d+l} : \text{realistic}$



TOOL now available in Sedfit
Le Roy et al., 2015

Practical: Ca⁺⁺ ATPase in DDM

Ca⁺⁺ ATPase: $M_{\text{monomer}}=109.49$ kDa $R_{\text{H}}=5.5$ nm $\bar{v}_{\text{p}}=0.7425$ ml/g $M_{\text{D}}/M_{\text{H}}=1.015$

$\epsilon_{280}=0.966$ cm⁻¹mLmg⁻¹ $\partial n/\partial c=0.187$ ml/g

DDM: $M_{\text{micelle}}\approx 67$ kDa $\bar{v}_{\text{det}}=0.82$ ml/g $M_{\text{D}}/M_{\text{H}}=1.014$

$\epsilon_{280}=0$ $\partial n/\partial c=0.143$ ml/g

solvents: $\eta_{\text{H}}=1.00$ cp $\rho_{\text{H}}=1.004$ g/mL $\eta_{\text{D}}=1.23$ cp $\rho_{\text{D}}=1.109$ g/mL

SV in H₂O (reference buffer without detergent):

absorbance + interference

$s_{\text{H}}/s_{\text{D}}$

SV of Ca⁺⁺ ATPase in DDM

- reference buffer without detergent, $\rho^{\circ}=1.004$, $\eta^{\circ}=1.00$

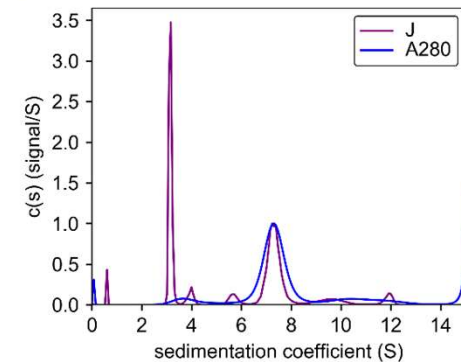
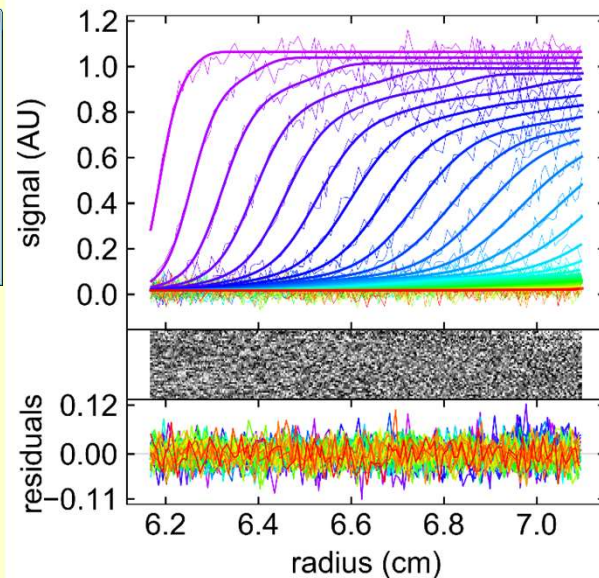
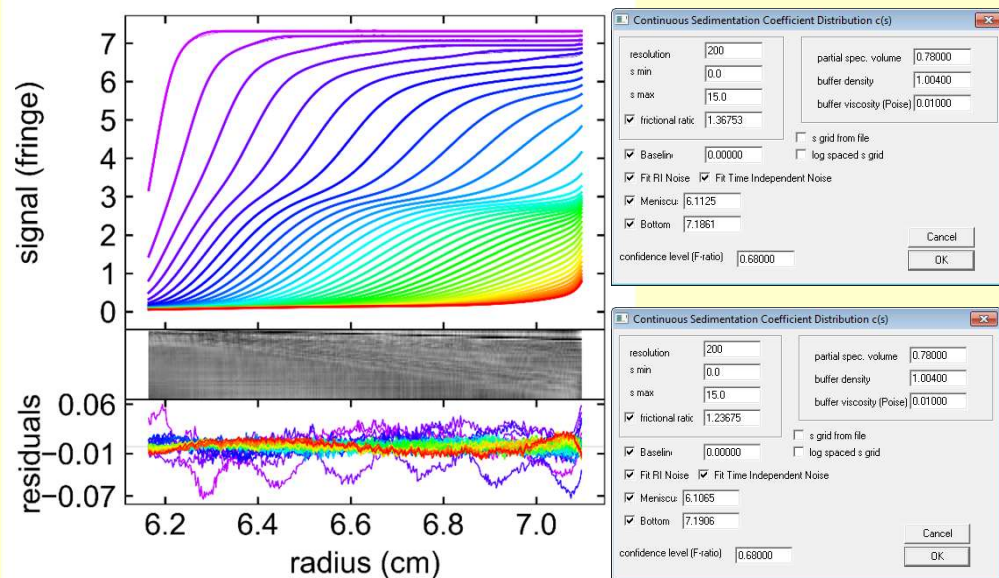
$c(s)$ analysis of interference than absorbance data (because detergent micelles moves slower)

- Selection of the files: => 80 first scans by 2
- Analysis with $\bar{v} = 0.78$ ml/g, intermediate between detergent and protein, s from 0 to 15S
- Fit f/f_{\min} , meniscus, and bottom, with resolution=50, F-ratio=0.5
Run with resolution=200, F-ratio=0.68

- => report f/f_{\min} values: => interference data: $f/f_{\min} = 1.37$; absorbance data: $f/f_{\min} = 1.24$

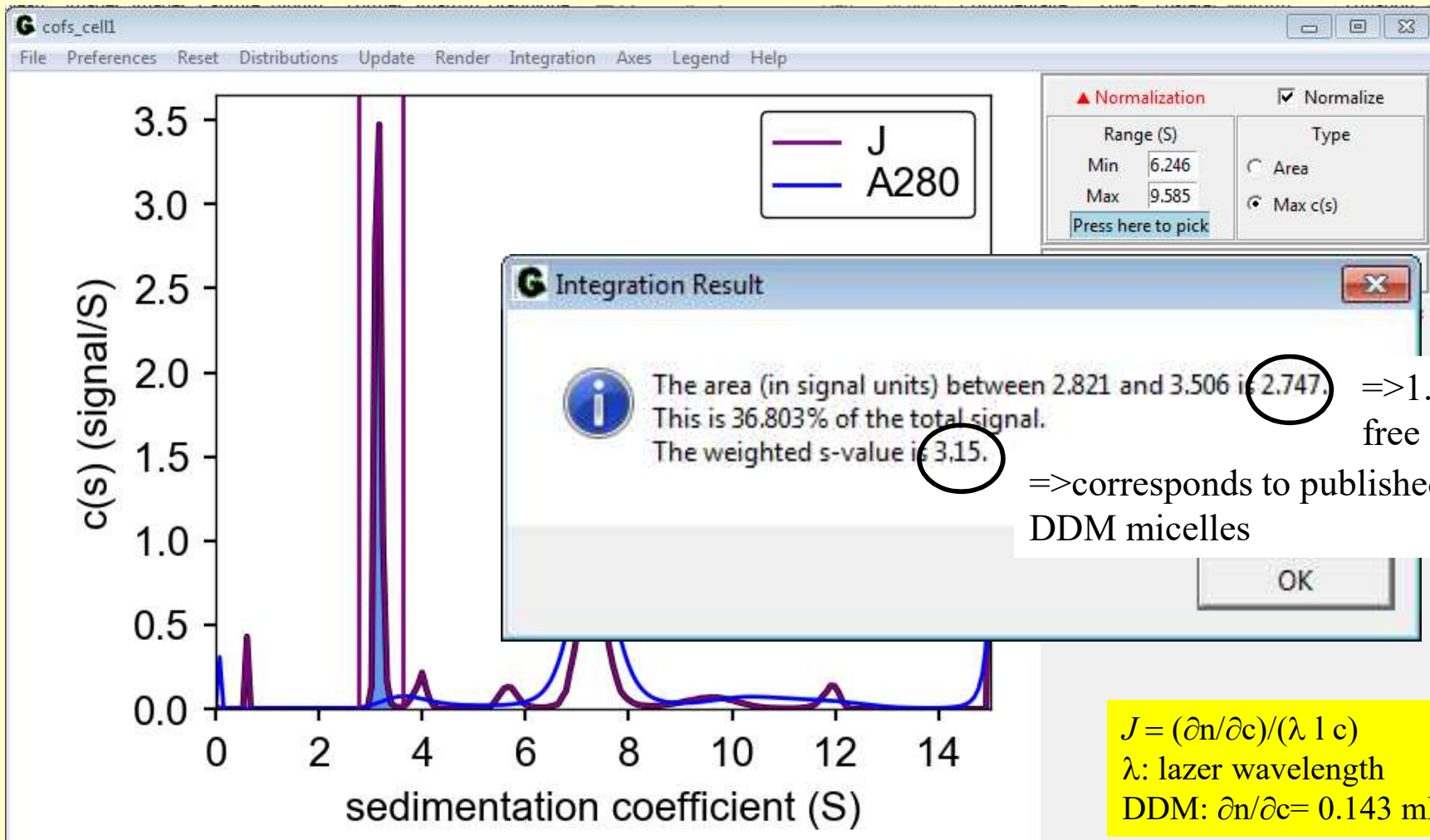
Note: f/f_{\min} here has no meaning because \bar{v} is not known, and there are different kind of particles

- =>Gussi data fit residual plot (save data only: ra1 scans, ip1 scans)
- =>Gussi $c(s)$ plot (save data only: ra1, ip1)
- => use gussi to superpose $c(s)$ from J and from A280, save as a gussi state (CaATPase)



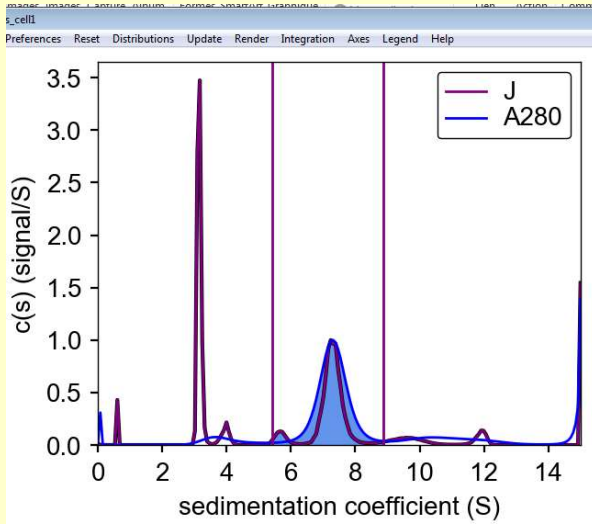
Estimation of free detergent micelle concentration

- Integration in e.g. GUSI of the detergent signal in the $c(s)$ from interference optics
- Using Excell sheet to calculate c from signal, optical path and $\partial n/\partial c$



Estimation of bound detergent and f/f_{min} for a given protein association state

- using gussi with $c(s)$ from Interf first, then from abs.: integrate/membrane protein calculation



Calculated from $c(s)$ integration

Input used to calculate bound detergent ($\epsilon_{det}=0$ by default)

Input used to calculate f/f_{min} , from s , M , and bound detergent

Experimental Parameters Used				
\bar{v} (cm ³ /g)	ρ (g/cm ³)	n (P)	T (K)	las. λ (nm)
0.78	1.004	0.0100	293	655

Protein Parameters				
ϵ (l/g·cm)	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	n-mer
0.966	0.7425	109490	0.187	1

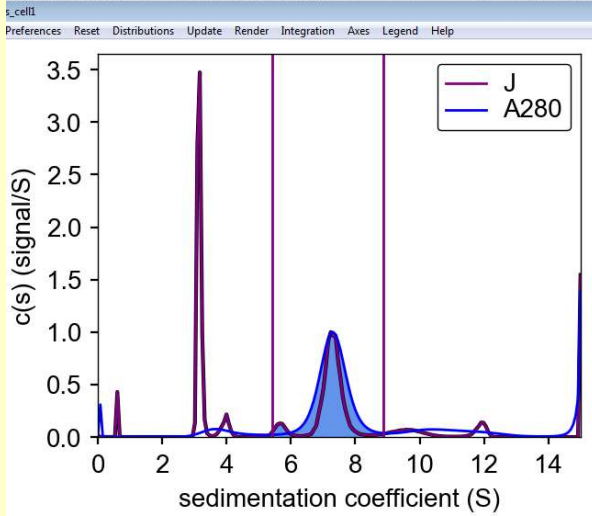
Detergent Parameters				
All det.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input checked="" type="checkbox"/>	0.82	200.0	0.143	0.609

Lipid Parameters				
All lip.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input type="checkbox"/>	0.98	200.0	0.14	0.0

Distributions					
distribution	s (S)	d (cm)	a	f/f ₀	det.
J (purple)	7.2	1.2	3.318	<input type="text"/>	IF
A280 (blue)	7.3	1.2	0.766	<input type="text"/>	ABS

Results: if monomer: the s -value, and the calculated bound detergent give $f/f_{min}=1.28$ =globular compact $RH=4.4$ nm. if dimer, $f/f_{min}=2$ = very elongated, $RH=8.9$ nm

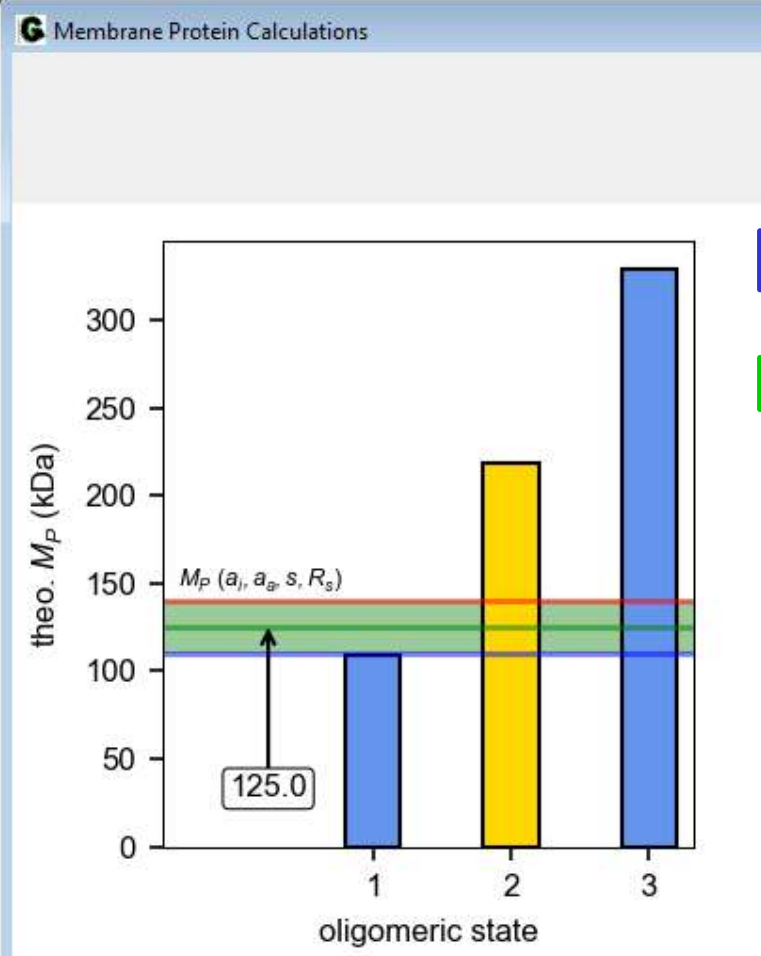
Estimation of bound detergent, then M when R_H is known



Calculated from $c(s)$ integration

Input used to calculate bound detergent ($\epsilon_{det}=0$ by default)

Input used to calculate M from s , R_H , and bound detergent



Membrane Protein Calculations

Calculation Type: f/f₀ fitted f/f₀ R_s (nm): 5.5

Experimental Parameters Used

\bar{v} (cm ³ /g)	ρ (g/cm ³)	η (P)	T (K)	las. λ (nm)
0.78	1.004	0.0100	293	655

Protein Parameters

ϵ (l/g·cm)	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	n-mer
0.966	0.7425	109490	0.187	2

Detergent Parameters

All det.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input checked="" type="checkbox"/>	0.82	200.0	0.143	0.609

Lipid Parameters

All lip.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input type="checkbox"/>	0.98	200.0	0.14	0.0

Distributions

distribution	s (S)	d (cm)	a	f/f ₀	det.
J (purple)	7.2	1.2	3.318		IF
A280 (blue)	7.3	1.2	0.766		ABS

Use f/f₀ from abs. only All data are ABS δ 's from user

Execute Save Figure View Report Dismiss

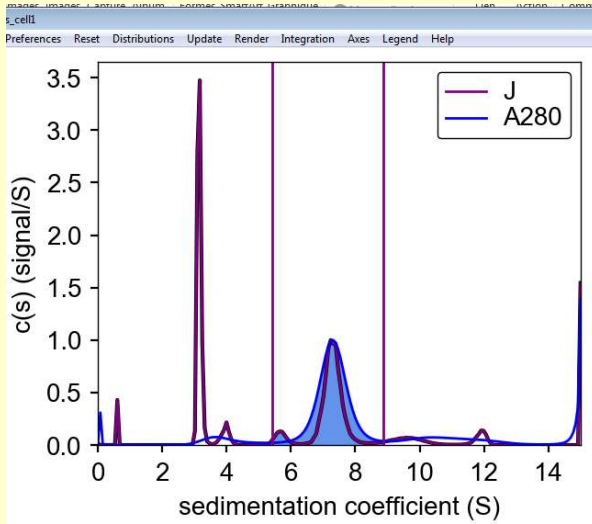
Save Params Load Params

Mouse Cursor Position

Stoich.	Mass
-0.0	322.5

Results: the s -value, and the calculated bound detergent, combined with $R_H=5.5$ nm, gives $M=125$ kDa, close to the monomer value (109 kDa)

Estimation of bound detergent and M given the f/f_{min} value calculated in sedfit



Calculated from $c(s)$ integration

Input used to calculate bound detergent

Input used to calculate M from s , f/f_{min} , and bound detergent

Experimental Parameters Used				
\bar{v} (cm ³ /g)	ρ (g/cm ³)	η (P)	T (K)	las. λ (nm)
0.78	1.004	0.010	293	655

Protein Parameters				
ϵ (l/g-cm)	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	n-mer
0.966	0.7425	109490	0.187	2

Detergent Parameters				
All det.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input checked="" type="checkbox"/>	0.82	200.0	0.143	0.609

Lipid Parameters				
All lip.	\bar{v} (cm ³ /g)	M (Da)	dn/dc (cm ³ /g)	δ (g/g)
<input type="checkbox"/>	0.98	200.0	0.14	0.0

Distributions					
distribution	s (S)	d (cm)	a	f/f_0	det.
J (purple)	7.2	1.2	3.318		IF
A280 (blue)	7.3	1.2	0.766	1.24	ABS

Results: using the D -calculated in sedfit (calculated from the apparent f/f_{min}), $M=107$ close to the monomer

From sH (usual buffer) and sD (buffer with heavy water, $\eta^\circ=1.23$ cp $\rho^\circ=1.109$ g/mL)

•In sedphat: options/interaction calculator/Ebel B-v Plot of detergent binding from Density contrast SV”

A graphical representation to investigate:

Is a given association state of the protein (monomer, dimer) compatible with the s- measured in H₂O and D₂O buffers?

Useful when lipid is bound in ill-defined amount

$$s_H = M_p \left[(1 - \rho_H \bar{v}_p) + \delta_d (1 - \rho_H \bar{v}_d) \right] / N_A 6\pi\eta_H R_s$$

$R_H=R_s$ is expressed as a function of the other above parameters, and of f/f_{\min} .

The program plots the mathematical solutions ($\delta_d ; v_d$) for $s_{H \min}$, $s_{H \max}$, $s_{D \min}$, $s_{D \max}$.

The area between these four curves gives the possible solutions ($\delta_d ; v_d$)

Plots have to be done for different oligomeric states, and f/f_{\min} .

In the deuterated buffer, the Svedberg equation is slightly modified to take into account the changes due to protein and detergent H/D exchange, modifying slightly the effective partial specific volume

$$s_D = M_p \left[\left(\frac{M_D}{M} \right)_p - \rho_D \bar{v}_p \right] + \delta_d \left[\left(\frac{M_D}{M} \right)_d - \rho_D \bar{v}_d \right] / N_A 6\pi\eta_D R_s$$

From sH (usual buffer) and sD (buffer with heavy water, $\eta^\circ=1.23$ cp $\rho^\circ=1.109$ g/mL)

• In sedphat: options/interaction calculator/Ebel B-v Plot of detergent binding from Density contrast SV”

smin (H2O) = 7.0

smax (H2O) = 7.2

smin (D2O) = 4.0

smax (D2O) = 4.2

eta(H2O) = 1.000

rho(H2O) = 1.004

eta(D2O) = 1.230

rho(D2O) = 1.109

MD/M (prof) = 1.0150

MD/M (bound)=1.0140

M (prof) = 109490

vbar (prof) = 0.743

plot vbar(min) = 0.700

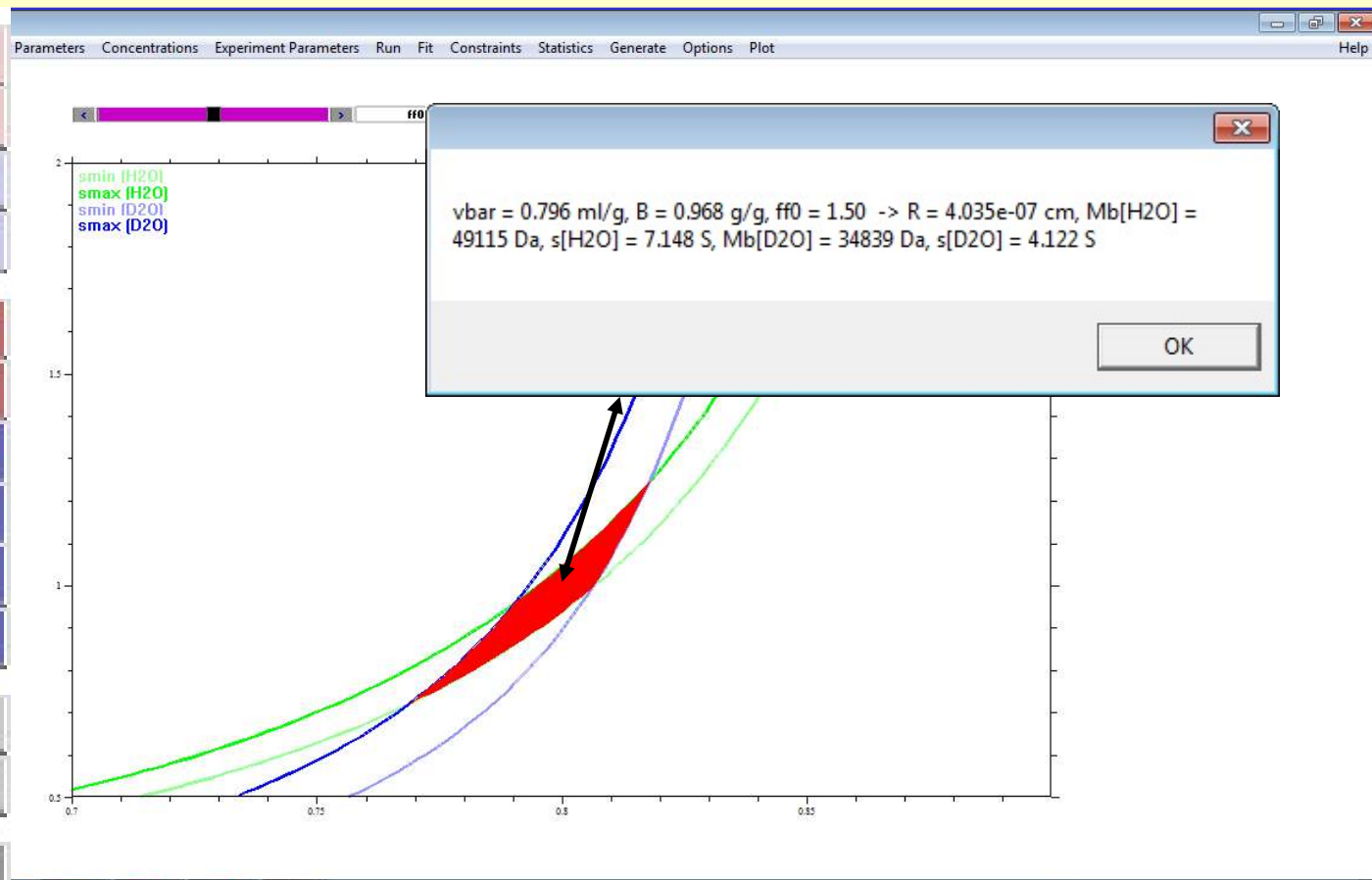
plot vbar(max) = 0.900

plot B(min) = 0.500

plot B(max) = 2.000

plot ff0(min) = 1.0

plot ff0(max) = 2.0



Results: for a monomer

With $fff_{\min} = 1.25$ $v_{\det} = 0.82 \pm 0.02$ mL/g, $B_{\det} = 0.45 \pm 0.15$ g/g

With $fff_{\min} = 1.5$: $v_{\det} = 0.80 \pm 0.02$ mL/g, $B_{\det} = 0.95 \pm 0.25$ g/g

With $fff_{\min} = 1.75$: $v_{\det} = 0.79 \pm 0.02$ mL/g, $B_{\det} = 1.5 \pm 0.3$ g/g

Dimer: $fff_{\min} > 1.8$, with $B_{\det} < 0.5$ g/g, $v_{\det} > 0.82$ mL/g, $R_s < 4.6$ nm

Questions?